ISSN 0081-5438, Proceedings of the Steklov Institute of Mathematics, 2024, Vol. 327, Suppl. 1, pp. S44-S65. © Pleiades Publishing, Ltd., 2024. Russian Text © The Author(s), 2024, published in Trudy Instituta Matematiki i Mekhaniki UrO RAN, 2024, Vol. 30, No. 3, pp. 293-313.

## Some Questions Related to the Extension of Reachability Problems in the Class of Finitely Additive Measures

## A. G. Chentsov<sup>1,2</sup>

Received April 4, 2024; revised May 5, 2024; accepted May 20, 2024

Abstract—Questions related to the extension of reachability problems and aimed at the construction of attraction sets, which are asymptotic analogs of reachable sets in the situation of successive relaxation of the constraint system, are studied. Finitely additive measures with the property of weak absolute continuity with respect to a fixed measure are used as generalized elements; the measure (in the case of control problems) is usually defined as the restriction of the Lebesgue measure to some family of measurable sets. The properties of relaxed reachability problems and the connection of their extensions with attraction sets in the class of ordinary solutions (controls), as well as the properties of these sets that have the sense of stability when the constraints are relaxed and asymptotic insensitivity when some "part" of the constraints is relaxed, are studied.

Keywords: finitely additive measure, attraction set, weak absolute continuity.

**DOI:** 10.1134/S0081543824070046

<sup>&</sup>lt;sup>1</sup>Krasovskii Institute of Mathematics and Mechanics, Ural Branch of the Russian Academy of Sciences, Yekaterinburg, 620108 Russia

 $<sup>^2</sup>$ Ural Federal University, Yekaterinburg, 620000 Russia e-mail: chentsov@imm.uran.ru