

An Optimal Control Problem with a Relaxed State Constraint

S. M. Aseev¹

Received July 8, 2024; revised July 26, 2024; accepted July 29, 2024

Abstract—We explore an optimal control problem in the context of a specified open set representing “undesirable” system states. This problem statement is closely linked to the standard optimal control problem with a state constraint and can be viewed as a relaxation of the latter. The interrelation between these problems is examined. Recently derived necessary first-order optimality conditions for the discussed problem are presented. An illustrative example is given.

Keywords: optimal control, differential inclusion, Pontryagin’s maximum principle, refined Euler–Lagrange inclusion, state constraint, discontinuous integrand, risk zone.

DOI: [10.1134/S0081543824070034](https://doi.org/10.1134/S0081543824070034)

¹Steklov Mathematical Institute of the Russian Academy of Sciences, Moscow, 119991 Russia
e-mail: aseev@mi-ras.ru