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## Conditions under Which the Sums of Absolute Values of Blocks in the Fourier–Walsh Series for Functions of Bounded Variation Belong to Spaces $L^p$

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**Abstract**—In this paper, the following question is considered: what conditions on a strictly increasing sequence of positive integers  $\{n_j\}_{j=1}^{\infty}$  guarantee that the sum of the series

$$\sum_{j=1}^{\infty} \left| \sum_{k=n_j}^{n_{j+1}-1} c_k(f) w_k(x) \right|,$$

where  $c_k(f)$  are the Walsh–Fourier coefficients of a function f, belongs to the space  $L^p[0,1)$ , p > 1, for any function f of bounded variation? For  $p = \infty$ , it is proved that such a sequence does not exist. For finite p > 1, sufficient conditions are obtained for the sequence  $\{n_j\}$ ; these conditions are similar to the ones obtained by the first author in the trigonometric case. **Keywords:** Walsh–Fourier series, functions of bounded variation,  $L^p$ -spaces.

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